









Total variance of measurement data :

$$\sigma_{\text{total}}^2 = \sigma_{\text{parts}}^2 + \sigma_{\text{R\&R}}^2$$

Fluctuation attributable to the measurement (precision):

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$$\sigma_{\rm R\&R}^2 = \sigma_{\rm reprod}^2 + \sigma_{\rm repeat}^2$$

Reproducibility:

$$\sigma_{\rm reprod}^2 = \sigma_{\rm oper}^2 + \sigma_{\rm part*oper}^2$$

Results:
• The variance components are related to the total variance.
• Analogously to the
$$C_p$$
 process capability index the ranges
attributed to the variance components is related to the width of
the spec. range (*P*/*T* precision to tolerance). Actually the 99%
(5.15 σ width) interval is in the numerator:

$$\frac{P}{T} = \frac{5.15 \cdot \hat{\sigma}_{R\&R}}{USL - LSL}$$
6.0 may stand for 5.15, expressing the ±3 σ limit (99.73% instead of 99%)
Number of distinguishable categories (discrimination index)

rounded down to integer

10

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 $rac{\hat{\sigma}_{
m part}}{\hat{\sigma}_{
m R\&R}}\sqrt{2}$

Design of experiments for the study A certain number (e.g. 10) is selected randomly from among the parts produced by the process to be investigated, all of them measured several (e.g. 3) times by each of the selected operators (e.g. 4).



operator	А				В					
part	rept 1	rept 2	rept 3	rept 1	rept 2	rept 3	rept 1	rept 2	rept 3]
1 2 3 4 5 6 7 8 9 10										
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Example

The width of the specification for the inner diameter 1.52 mm. 10 parts are taken randomly from the manufacturing, each of them are measured 3 times by 2 operators.

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Perform a Gauge R&R study!





Variance Components; Variable: micro (micro.sta)											
	Mean=483.535 Std.Dv=.119260										
	Operators: 3 Parts: 10 Trials: 3										
Source Estimatd .90		.90 Lowr	.90 Up	or Esti	imatd	% of	%	of			
(Expected MS) Sigma Cor		Conf.Lim	Conf.Lir	n Vari	ance	R & R	To	tal			
Repeatability 0.026055 0.0		0.022695	0.0307	11 0.0	00679	6.2345	5 3.	9321			
Operator 0.085921 0.		0.043097	0.3861	96 0.0	07382	67.7951	42.	7588			
Interaction (OP)	nteraction (OP) 0.053179 0.4		0.0770	27 0.0	02828	25.9704	16.	3797			
Part-to-Part	art-to-Part 0.079849 0.0		0.1444	58 0.0	06376		36.	9294			
Combined R & R	ombined R & R 0.104352 0.0		0.3912	56 0.0	10889	100.0000) 63.	0706			
Total	0.131397			0.0	17265		100.	.0000			
			Quic	Advan	ced Des	criptives/plo	ots Ga	ige performar	nce Options		
			-								
Range method variance estimate											
	HIII Hange method percent tolerance										
	Percen	Percent Tolerance Analysis:micro Sigma intervals:6. (micro.sl							1		
	Mean=	Mean=483.535 Std.Dv=.119260									
	Operat	Operators: 3 Parts: 10 Trials: 3							-		
Source	Measr	mnt .9) Lowr	.90 Up	pr % P	roc.	% Total	% of			
(Expected MS)		Uni	ts Co	nf.Lim	Conf.L	im Vari	atn	Contrib.	Tolernce		
Repeatability (Equip	Repeatability (Equipment Var).		6333 0	136172	0.184	266 19.	.8296	3.9321	10.2851		
Operator (Appraiser Var.)		0.51	5525 0	258584	2.317	176 65.	3902	42.7588	33.9161		
Interaction (Operator x Part)		0.31	9073 0	231688	0.462	160 40.	4718	16.3797	20.9916		
Part Variation		0.47	9096 0	267801	0.866	750 60.	7695	36.9294	31.5195		
Combined R & R		0.62	6110 0	455672	2.347	534 79.	4170	63.0706	41.1914		
Total Process Variat	0.78	0.788382			100.	.0000	100.0000	51.8673			
I olerance	1.52	1.520000						100.0000			
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