### 4. ENZYME KINETICS



#### **Enzyme kinetics**

Investigation of enzymatic reaction rate, identification of parameters.

$$E + S \leftrightarrow E + P$$

For stoichiometric calculations all components should be given in moles or grams. But: enzymes are not pure proteins!  $\rightarrow$  amount of enzymes is measured through their catalytic effect  $\rightarrow \underline{ACTIVITY}$ 



#### **Enzyme kinetics**

One **UNIT** is the amount of the enzyme which consumes 1  $\mu$ mol substrate or forms 1  $\mu$ mol product during 1 minute *at given reac-tion circumstances*.

- SI: 1 Katal: 1 mol substrate (product) during 1 s. (too huge!!)  $\rightarrow$  nKat = 10<sup>-9</sup> Kat (nanoKatal)
  - 1 Kat =  $6^{*}10^{7}$  U, 1 U =  $1.666^{*}10^{-8}$  Kat, 1 U = 1/60 µKat, 1 U = 16.67 nKat

**Specific activity**: U/mass or U/volume  $\rightarrow$  U/mg, U/ml



$$E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$$

Conditions:

- $\succ$  k<sub>-2</sub> = 0 (the second step is irreversible)
- the first step reaches the equilibrium quickly =
   RAPID EQUILIBRIUM: k<sub>1</sub>SE = k<sub>-1</sub> (ES)

Dissociation constant of (ES):

$$K_{s} = \frac{k_{-1}}{k_{1}} = \frac{S.E}{(ES)}$$

stable ES complex, EP complex negligible



$$E + S \stackrel{k_1}{=} ES \stackrel{k_2}{=} E + P$$

one active centre, one substrate

concentration can be applied (instead of activity)
 (S) >> (E<sub>0</sub>) i.e. E<sub>0</sub> / S << 1</li>

Reaction rate:

$$V = \frac{dP}{dt} = k_2(ES)$$

Mass balance for E:  $E + (ES) = E_o$ 

Divide these equations!







#### The rate equation:

$$V = V_{max} \frac{S}{K_s + S} \quad \text{or} \quad \frac{V}{V_{max}} = \frac{\frac{S}{K_s}}{1 + \frac{S}{K}}$$



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## M és M





#### Maud Menten 1879-1960

Leonor Michaelis 1875-1949

Michaelis, L., Menten, M. (1913) Die kinetik der invertinwirkung, Biochemische Zeitung 49, 333-369



## **Briggs-Haldane kinetics**

$$E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$$

#### The same differential equtions but the condition:

$$\frac{\mathrm{dS}}{\mathrm{dt}} = -k_1 \mathrm{ES} + k_{-1} \mathrm{(ES)}$$

(quasi) steady state:

d(ES)/dt = 0

$$\frac{d(ES)}{dt} = k_1 ES - k_{-1} (ES) - k_2 (ES)$$

(S) >> (E<sub>0</sub>) i.e.  $E_0/S << 1$  $k_1ES > k_{-1}(ES)$  ill.  $k_1ES > k_2(ES)$ 



 $\frac{\mathrm{dP}}{\mathrm{dt}} = \mathbf{k}_2 \left( \mathbf{ES} \right)$ 

# **Briggs-Haldane kinetics**

After a short transition period (pre-steady state) the rate is almost constant (quasi-steady state).



Briggs, G. E., and Haldane, J. B. (1925) A Note on the Kinetics of Enzyme Action, *Bio-chem J 19*, 338-339.



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#### **Briggs-Haldane kinetics**





#### Discussion

#### Michaelis-Menten

$$V = V_{max} \frac{S}{K_s + S}$$

$$\mathbf{K}_{\mathrm{s}} = \frac{\mathbf{k}_{-1}}{\mathbf{k}_{1}}$$

#### Briggs-Haldane

$$V = V_{max} \frac{S}{K_m + S}$$

$$\mathbf{K}_{\mathrm{m}} = \frac{\mathbf{k}_{-1} + \mathbf{k}_2}{\mathbf{k}_1}$$

$$\mathbf{K}_{\mathrm{m}} = \mathbf{K}_{\mathrm{s}} + \frac{\mathbf{k}_{2}}{\mathbf{k}_{1}}$$

if  $(k_1) >> (k_2)$  the two constants are equal!



#### Discussion



# Hyperbola



#### How to measure reaction rate?

In M-M and B-H equations V means initial reaction rate  $(V_0 \rightarrow \text{extrapolated to t=0})$ .





#### Parameter estimation

Linearised diagrams are used:

- Calculation of nonlinear regression was complicated without computers
- It provides additional info about enzyme inhibition

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1. Lineweaver-Burk plot

1/v - 1/S





# Linearised forms

2. Hanes-Langmuir plot S/v - S

$$\frac{S}{V} = \frac{K_m}{V_{max}} + \frac{1}{V_{max}} \cdot S$$

3. Eady-Hofstee plot v/S - v

$$V = V_{max} - K_m \frac{V}{S}$$





/S

#### Effect of enzyme concentration

If  $v_{max} = k_2 \cdot E_0$ , then:



### Interpretation of kinetic parameters

 $V_{max}$ : its not a climax, but limit  $\rightarrow$  border of rate

It's not an enzyme feature, it depends on  $E_0$ :

 $V_{max} = k_2 \cdot E_0 \rightarrow = \mathbf{ACTIVITY}$ 

 $\mathbf{k_2}$  is the real enzyme feature = turnover number  $[s^{-1}] \rightarrow$ 

transformation frequency

Extending to every enzymes and every kinetics:

$$V_{max} = k_{cat} \cdot E_0$$

 $\mathbf{k}_{cat}$  [s<sup>-1</sup>]: Turnover frequency of one enzyme molecule (at S-saturation): how many substrate molecules are transformed in one second by one enzyme molecule.



# Kinetic parameters: K<sub>s</sub>, K<sub>m</sub>

- > Affinity of enzyme to substrate
- Usually the S concentration in a living cell easy adaption to changes
- $\succ$  K<sub>S</sub> has changed  $\rightarrow$  Inhibitor? Activator?
- Enzyme analytics:
- activity measurement:
  - S>>K<sub>S</sub> v=v<sub>max</sub>
- substrate measurement:
  - S<<K<sub>S</sub> linear range



# Interpretation of kinetic parameters

| k <sub>1</sub>  | 10 <sup>7</sup> -10 <sup>10</sup> dm <sup>3</sup> mol <sup>-1</sup> min <sup>-1</sup> [max. value (~10 <sup>11</sup> ) |
|-----------------|--|
|                 | limited by diffusivity of small molecules]   |
| k <sub>-1</sub> | 10 <sup>2</sup> -10 <sup>6</sup> min <sup>-1</sup>   |
| $k_2$           | 50-10 <sup>7</sup> min <sup>-1</sup>   |
| κ <sub>m</sub>  | 10 <sup>-6</sup> - 10 <sup>-2</sup> mol/dm <sup>3</sup>  |

#### TABLE 13-1. The values of $K_M$ , $k_{cat}$ , and $k_{cat}/K_M$ for Some Enzymes and Substrates

| Enzyme               | Substrate   | $K_M(M)$   | k <sub>cat</sub> (s <sup>-1</sup> )                                 | $k_{\rm cat}/K_M (M^{-1}{ m s}^{-1})$              |
|----------------------|---|--|---|--|
| Acetylcholinesterase | Acetylcholine   | 9.5 × 10 <sup>−5</sup>   | $1.4 \times 10^{4}$   | 1.5 × 10 <sup>8</sup>                              |
| Carbonic anhydrase   | CO <sub>2</sub><br>HCO <sub>3</sub>   | $1.2 \times 10^{-2}$<br>$2.6 \times 10^{-2}$                         | $1.0 	imes 10^{6}$<br>$4.0 	imes 10^{5}$                            | $8.3 \times 10^{7}$<br>$1.5 \times 10^{7}$         |
| Catalase             | H <sub>2</sub> O <sub>2</sub>   | 2.5 × 10 <sup>-2</sup>   | $1.0 \times 10^{7}$   | $4.0	imes10^{8}$                                   |
| Chymotrypsin         | N-Acetylglycine ethyl ester<br>N-Acetylvaline ethyl ester<br>N-Acetyltyrosine ethyl ester | $4.4 \times 10^{-1}$<br>$8.8 \times 10^{-2}$<br>$6.6 \times 10^{-4}$ | $5.1 \times 10^{-2}$<br>$1.7 \times 10^{-1}$<br>$1.9 \times 10^{2}$ | $1.2 \times 10^{-1}$<br>1.9<br>$2.9 \times 10^{5}$ |
| Fumarase             | Fumarate<br>Malate  | $5.0 \times 10^{-6}$<br>$2.5 \times 10^{-5}$                         | $8.0 \times 10^2$ $9.0 \times 10^2$                                 | $1.6 \times 10^{8}$<br>$3.6 \times 10^{7}$         |
| Urease               | Urea  | $2.5 \times 10^{-2}$   | $1.0 \times 10^{4}$   | $4.0 	imes 10^{5}$                                 |







#### **Reversible reactions**

Many enzyme catalysed reactions - mainly biopolymer hydrolysis - are highly shifted to the right hand side, practically  $k_{-2}$  may really be neglected.

But conversions like

glucose ⇒ fructose (glucose isomerase) ~50 : 50 %

#### are of reversible character.



#### **Reversible reactions**

While  $k_{-2} = 0$  in both kinetic models reactions seems to be irreversible. Models for reversible (equilibrium) reactions are built up from models of two countercurrent irreversible reaction.





Presume the presence of EP complex:

$$E + S \rightleftharpoons ES \rightleftharpoons EP \rightleftharpoons E + P$$
$$k_{-1} \quad k_{-2}$$



#### **Reversible reactions**

The netto rate is the difference of the two processes:

$$V_{\text{netto}} = V_{\text{fore}} - V_{\text{back}} = k_2 (\text{ES}) - k_{-2} (\text{EP})$$

Repeat the previous deduction, divide the equation with:

$$E_{o} = E + (ES) + (EP)$$

$$\frac{v_{fore}}{E_{o}} = \frac{k_{2}(ES)}{E + (ES) + (EP)} \qquad \frac{v_{back}}{E_{o}} = \frac{k_{-2}(EP)}{E + (ES) + (EP)}$$

From these:

$$\Delta v = \frac{E_0 k_2 (ES) - E_0 k_{-2} (EP)}{E + (ES) + (EP)}$$



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#### **Reversible reactions**

Substitute v<sub>max</sub>:

$$\Delta v = \frac{v_{\max S}(ES) - v_{\max P}(EP)}{E + (ES) + (EP)}$$

Substitute complex concentrations:

$$(ES) = E \frac{S}{K_s} \qquad (EP) = E \frac{P}{K_P}$$

$$\Delta v = \frac{v_{\max S} \frac{S}{K_s} E - v_{\max P} \frac{P}{K_p} E}{E + \frac{S}{K_s} E + \frac{P}{K_p} E}$$
equa

$$= S_{equilibrium}$$

$$\Delta V = \frac{V_{maxs} \left( S \left( \frac{P}{K_{eq}} \right) \right)}{K_{ms} \left( 1 + \frac{P}{K_{mp}} \right) + S}$$

**Reversible M-M equation** 

